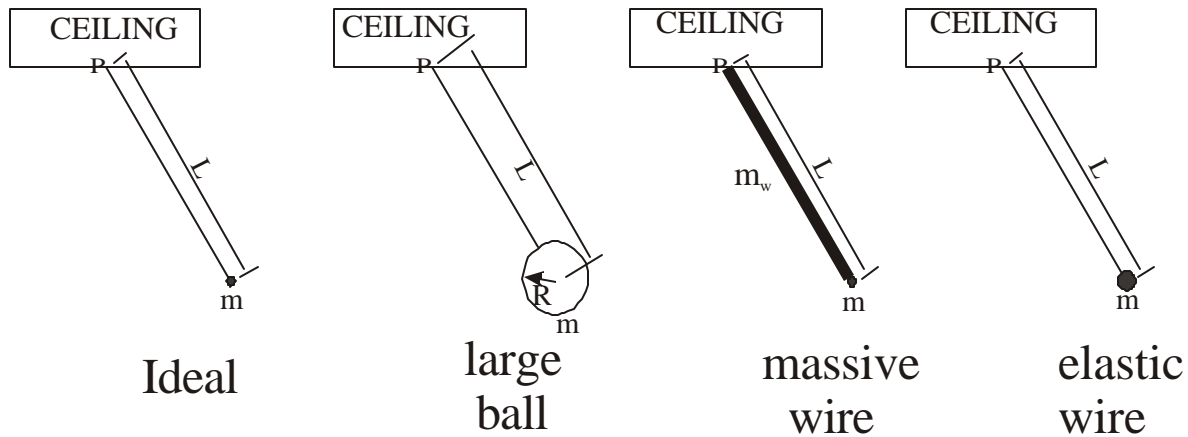


**Quiz 01-03**

A simple pendulum ideally consists of a massive object of infinitesimally small dimensions attached at one end of a massless inextensible (will not stretch) string or wire. The cord is attached to a supporting structure at point P. When attempting to determine the effects of non-ideal situations, it is best to take them one at a time. The picture shows the a) the ideal, b) large ball where R that is not infinitesimally small compared to L, c) the wire or string has mass  $m_w > 0$ , d) the wire or string is elastic with a Young's Modulus  $M_Y$ .



**1. Massless string or wire, large ball , inelastic (no stretch) wire**

$R$  = radius of ball,  $L$  = length from support to center of ball

$$\tau_p = m L g \theta$$

$$I_p = mL^2 + 2/5 mR^2$$

$$T = T_0 (1 + 2/5 (R/L)^2)^{1/2}, \quad \text{where } T_0 = 2\pi (L/g)^{1/2}$$

A. Verify that  $I_p$  is as given above.

B. Derive the expression for  $T$

**2. Massive string or wire , small ball, inelastic (no stretch) wire**

$m$  = mass of ball ,  $m_w$  = mass of wire or string

$$\tau_p = (m_w L/2 + mL)g \theta \quad I_p = 1/3 m_w L^2 + mL^2$$

$$T = T_0 \{ ( (1 + [1/3] [m_w/m]) / ( 1 + [1/2] [ m_w/m ] ) ) \}^{1/2}$$

A. Verify that  $I_p$  is as given above.

B. Verify the expression for  $\tau_p$

C. Derive the expression for  $T$

**3. Massless string, small ball, elastical (stretches) wire**

$M$  = mass of ball ,  $L$  = length from support to center of ball,

$M_Y$  = Young's Modulus of the string or wire material

$$\tau_p = mLg \theta \quad I_p = mL^2$$

$$\Delta L = L_0 F / (AM_Y) \quad A = \text{cross section area of wire,}$$

$$F = \text{weight on wire} = \text{weight of ball} = mg$$

$$T = T_0 ( 1 + mg/[AM_Y] )^{1/2} \quad , \text{ where } T_0 = 2\pi (L_0/g)^{1/2}$$

A. Derive the expression for  $T$ .

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